Reg. No. : $\qquad$
Name : $\qquad$

# Third Semester B.Sc. Degree Examination, March 2021 First Degree Programme under CBCSS 

Physics

## Complementary Course for Mathematics

## PY 1331.1 : OPTICS, MAGNETISM AND ELECTRICITY

 (2019 Admission Regular)Time : 3 Hours
Max. Marks : 80
PART - A

Answer all the questions. Answer should not exceed 2 sentences. Each question carries 1 mark.

1. What is interference?
2. Explain the phenomenon behind diffraction.
3. How is Newton's ring formed?
4. What is the principle behind the working of a LASER?
5. What is an optical pumping? give example
6. Name four elements which exhibit paramagnetism.
7. Define the term magnetic permeability.
8. What do you mean by resonant frequency?
9. What is the practical application of a series LCR circuit?
10. What do you mean by power factor?

$$
(10 \times 1=10 \text { Marks })
$$

PART - B

Answer any eight questions. Answer should not exceed one small paragraph. Each question carries 2 marks.
11. Write note on the comparison of prism spectra and grating spectra.
12. What is Fraunhoffer diffraction?
13. State the principle of superposition of waves.
14. What do you understand by
(a) fringes of equal thickness
(b) fringes of equal inclination?
15. Explain briefly about spontaneous emission.
16. Write a short note on magnetic susceptibility.
17. Compare the magnetic properties of diamagnetic, paramagnetic and ferromagnetic materials.
18. Write note on population inversion.
19. Write note on ferromagnetism.
20. Briefly explain about choke coil and its applications.
21. Write note on stimulated emission.
22. Explain about the resolving power of a plane diffraction grating.
23. What do you mean by the dispersive power of a grating? On what factors do it depends.
24. What do you mean by fringe width of interference? On what factors do it depends on?
25. With a neat diagram explain about the series RC circuit.
26. Mention the uses of transformers.

$$
\text { ( } 8 \times 2=16 \text { Marks })
$$

PART - C

Answer any six questions. Each question carries 4 marks.
27. In a Newton's rings experiment with air film the diameter of the $\mathrm{m}^{\text {th }}$ dark ring is 0.577 cm . With a liquid film the same arrangement gives similar rings but the diameter of the $\mathrm{m}^{\text {th }}$ ring becomes 0.434 cm . Find the refractive index of the liquid.
28. A parallel beam of light of wavelength $4500 \AA$ is incident at an angle of $30^{\circ}$ on a plane transmission grating which has 9000 lines $/ \mathrm{cm}$. find the highest order spectrum that can be observed.
29. Light of wavelength $6000 \AA$ is incident on a narrow slit of width 0.30 mm . The screen is placed 2 m away from the slit. Find (a) the position of the first dark fringe and (b) the width of the central bright fringe.
30. Two coherent are 0.15 mm apart and the fringes are observed on a screen 50 cm away. It is found that with a certain monochromatic source of light; the fourth bright fringe is situated at a distance of 10.5 mm from the central fringe. Calculate the wavelength of light.
31. If the number of lines per millimetre of a grating is 589 , how many orders of spectra are possible for light of wavelength $6.00 \times 10^{-7} \mathrm{~m}$ ?
32. A soft iron ring has a mean diameter of 0.2 m and an area of cross section of $5 \times 10^{-4} \mathrm{~m}^{2}$. It is uniformly wound with a coil of 2000 turns and a current of 2 A is passed through it. The magnetic flux produced in the iron ring is $8 \times 10^{-3} \mathrm{~Wb}$. Calculate the relative permeability of iron.
33. A step down transformer is connected to a mains supply of 220 volts is made to operate a 12, volt 40 watt bulb. lgnoring the energy losses, calculate (a) current in the primary coil (b) transformation ratio, assuming that there is no loss of power.
34. Find the natural frequency of a circuit containing an inductance of $50 \mu \mathrm{H}$ and capacitor of capacity $0.001 \mu \mathrm{~F}$.
35. An AC of 180 volts and 100 Hz is fed to a circuit containing a resistance R and capacitance $C$ connected in series. Calculate the values of $R$ and $C$ when the maximum current is 5 A and active power is 300 watts.
36. Find the numerical aperture and acceptance angle of a core index 1.5 and $\Delta=0.05$.
37. A step-index fiber has a core index of refraction of $n_{1}=1.425$. The cut-off angle. for light entering the fiber from air is found to be $8.50^{\circ}$. Calculate (a) numerical aperture ( $b$ ) index of refraction of the cladding (c) If the fiber were submersed in water, what would be the new numerical aperture and cut-off angle? [given $\mathrm{n}_{\text {air }}=1.0003$ ]
38. In a series RLC, circuit $R=30 \Omega, L=15 \mathrm{mH}$, and $\mathrm{C}=51 \mu \mathrm{~F}$. If the source voitage and frequency are 12 V and 60 Hz , respectively, what is the current in the circuit?
( $6 \times 4=24$ Marks $)$
PART - D

Answer any two questions. Each question carries 15 marks.
39. Describe briefly about the light propagation in optical fibre and mention its applications.
40. Explain the electron theory of magnetism and the explanation of ferromagnetism.
41. Explain with the neat diagram the series LCR circuit and its resonance.
42. Explain the theory of interference and conditions for maximum and minimum intensities with equations.
43. Explain the Fresnel's diffraction at straight edge and discuss the pattern.
44. Comment on the long distance power transmission, transformers and its uses.
( $\mathbf{2} \times 15=30 \mathrm{Marks}$ )

Reg. No. : $\qquad$
Name: $\qquad$

# Third Semester B.Sc. Degree Examination, March 2021 

First Degree Programme under CBCSS

## Mathematics

Core Course - II

## MM 1341 : ELEMENTARY NUMBER THEORY AND CALCULUS - I

## (2018 Admission)

Time : 3 Hours
Max. Marks : 80

## SECTION I

All the questions are compulsory. Each question carries 1 mark.

1. State the Inclusion-Exclusion Principle for 3 finite sets $A, B$ and $C$.
2. Define a Linear Diophantine Equation in two variables.
3. Define Derivative of a vector-valued function $r(t)$.
4. Evaluate the definite integral, $\int_{0}^{2} 2 t i+3 t^{2} j d t$.
5. Define Unit Normal Vector.
6. Give the formula for $a_{N}$, the normal component of acceleration for a moving particle in terms of the velocity $v$ and the acceleration $a$.
7. Find the natural domain of $f(x, y, z)=\sqrt{1-x^{2}-y^{2}-z^{2}}$.
8. Define an Open set.
9. Define Gradient of a function $f(x, y, z)$.
10. State the Extreme value theorem.

## SECTION II

Answer any eight questions. Each question carries 2 marks.
11. State and prove the Pigeonhole Principle.
12. Express $3 A B C_{\text {sixteen }}$ in base 10 .
13. Find $(4076,1024)$.
14. Prove that two integers $a$ and $b$ are relatively prime if and only if $[a, b]=a b$.
15. Let $r(t)=t^{2} i+e^{t} j-(2 \cos \pi t) k$. Find $\lim _{t \rightarrow 0} r(t)$.
16. Define a tangent vector and tangent line through the point $P$ on the graph of a vector-valued function $r(t)$.
17. State the chain rule for differentiation of vector functions.
18. A particle moves through 3-space in such a way that its velocity is $v(t)=i+t j+t^{2} k$. Find the coordinates of the particle at time $t$.
19. Define Level surfaces and find the level surfaces of $f(x, y, z)=z^{2}-x^{2}-y^{2}$.
20. Define local linear approximation to $f(x, y)$ at $\left(x_{0}, y_{0}\right)$.
21. Consider the ellipsoid $x^{2}+4 y^{2}+z^{2}=18$. Find an equation of the tangent plane to the ellipsoid at the point $(1,2,1)$.
22. Explain the steps to find the absolute extrema of a continuous function $f$ of two variables on a closed and bounded set $R$.

## SECTION III

Answer any six questions. Each question carries 4 marks.
23. Find the number of integers $\leq 3000$ and divisible by 3,5 or 7 .
24. Prove that if $a$ and $b$ are positive integers, then $[a, b]=\frac{a b}{(a, b)}$.
25. Using canonical decomposition, find the LCM of 1050 and 2574.
26. Find parametric equations of the tangent line to the circular helix $x=\cos t, y=\sin t, z=t$ where $t=t_{0}$, and use that result to find parametric equations for the tangent line at the point where $t=\pi$.
27. If $r_{1}(t)$ and $r_{2}(t)$ are two vector functions of $t$, derive the expression for $\frac{d}{d t}\left(r_{1} \times r_{2}\right)$.
28. Find $r(t)$ given that $r^{\prime}(t)=(3,2 t)$ and $r(1)=(2,5)$.
29. Assuming that polynomials in one variable and cosine function are continuous, show that $f(x, y)=\cos \left(3 x^{3} y^{4}\right)$ is continuous everywhere. State the results used for the proof.
30. Differentiability of function $f(x, y)$ at a point implies continuity at that point. Justify the statement.
31. Suppose that $w=x^{2}+y^{2}-z^{2}$ and $x=\rho \sin \varphi \cos \theta, y=\rho \sin \varphi \sin \theta, z=\rho \cos \varphi$ use appropriate forms of the chain rule to find $\frac{\partial w}{\partial \rho}$ and $\frac{\partial w}{\partial \theta}$.

## SECTION IV

Answer any two questions. Each question carries 15 marks.
32. (a) State and Prove the Fundamental Theorem of Arithmetic.
(b) Let $b \geq 2$ be an integer and $b+1$ integers are randomly selected. Prove that the difference of two of them is divisible by $b$.
33. (a) If a circle is parameterised by arc length as

$$
r(s)=a \cos \left(\frac{s}{a}\right) i+a \sin \left(\frac{s}{a}\right) j(0 \leq s \leq 2 \pi a) . \text { Find } T(s) \text { and } N(s) .
$$

(b) Find the curvature $k(t)$ for the circular helix $x=a \cos t, y=a \sin t, z=c t$ where $a>0$.
34. Given $f(x, y)=\frac{x y}{x^{2}+y^{2}}$, find the limit of $f(x, y)$ as $(x, y) \rightarrow(0,0)$ along
(a) The $x$-axis
(b) The y-axis
(c) The line $y=x$
(d) The line $y=-x$
(e) The parabola $y=x^{2}$.
35. Explain Lagrange multipliers Method and use it to determine the dimensions of a rectangular box, open at the top, having a volume of $32 \mathrm{ft}^{3}$, and requiring the least amount of material for its construction. Given the surface area being $S=x y+2 x z+2 y z$.

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Third Semester B.Sc. Degree Examination, March 2021 First Degree Programme under CBCSS

Physics
Complementary Course for Mathematics
PY 1331.1 : OPTICS, MAGNETISM AND ELECTRICITY
(2019 Admission Regular)
Time: 3 Hours

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\text { (10 } \times 1=10 \text { Marks) }
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$$
(2 \times 15=30 \text { Marks })
$$

Reg. No. : $\qquad$
Name : $\qquad$
Third Semester B.A./B.Sc. Degree Examination, March 2021
First Degree Programme Under CBCSS
English - (Language Course)
EN 1311.1/EN 1311.3 : ENGLISH FOR CAREER (Common for B.A./B.Sc. and Career Related 2(a))
(2019 Admission, Regular)
Time: 3 Hours
Max. Marks : 80 .
I. Answer all the following questions. Follow the instructions given in the brackets wherever needed.

1. The correct spelling of the word 'exibition' is $\qquad$
2. The word that is the antonym of "economical" is $\qquad$
3. 'Fragrance' is a word related to the sense of $\qquad$
4. $\qquad$ is the noun form of 'emigrate'.
5. It $\qquad$ (be) an honour for him to lead and serve the company. (Use the correct tense form of the verb in brackets)
6. Do you know where is the church. (Correct the sentence)
7. What number of students are in this class? (Underline the error)
8. The term 'epidemiological' is related to the study of $\qquad$
9. How much costs it to buy a diamond necklace?
(Correct the sentence)
10. They had to $\qquad$ the meeting yesterday due to the sudden bus strike. (Use the appropriate phrasal verb which means "cancel or stop")
(a) Call up
(b) Call for ${ }^{\circ}$
(c) Call off
(d) None of these
(10 $\times 1$ = 10 Marks)
II. Answer any eight of the following questions.
11. Provide one word substitutes for any two of the phrases
(a) Stood up and applauded
(b) A piece of writing about the writer's journeys to different places
(c) A person who collects stamps
(d) A person who walks in her/his sleep
12. Give the antonyms of two of the following words
(a) convergence
(b) sensibility
(c) unknown
13. Give the synonym of two of the following words
(a) hilarious
(b) outlook
(c) modify
14. Make sentences of your own with any two of the following phrasal verbs
(a) ran into
(b) turned up
(c) to make light of
(d) made off with
15. Choose the correct option from the brackets :
(a) The Manager all the claims of the employee and dismissed him. (reputed / refuted).
(b) I suppose the headmaster himself will $\qquad$ the matter now. (look into / look out for)
16. Fill in the blanks using a collective noun from those given below (band, pride, herd, bunch, clutch) :
(a) We saw a $\qquad$ of elephants moving across the river bed.
(b) The rock $\qquad$ has been on tour for months.
17. Fill in the blanks using the suitable degree of the adjective given in brackets :
(a) Lead is $\qquad$ than any other metal. (heavy)
(b) He thinks he is $\qquad$ than his father. (wise)

Correct the error in the words / phrases given in italics:
18. (a) Poorness is not an enviable condition.
(b) Here are the mangoes; please don't take this that are rotten.
19. (a) Suman studied in a girls' school till her tenth class.
(b) Can you give me some informations on the uses of lasers?
20. (a) Environmental degradation is a pereniel problem for humans today.
(b) My cousin likes fruits of forin countries.
21. (a) Your targets are to achieving before the end of this month.
(b) The clothes were all washed and hanged out to dry.
22. Fill in the blanks with suitable words from those given in brackets. (when, enough, leisurely, rather)
(a) He is a $\qquad$ careless fellow.
(b) These are days $\qquad$ no one can have a sense of security.
(c) He was foolish $\qquad$ to believe her.
(d) I had a $\qquad$ walk.
23. Fill in the blanks with suitable words from those given in brackets. (medical, deliberate, grand, constant)
(a) The battle of Waterloo ended in a $\qquad$ victory.
(b) The injured man wants $\qquad$ advice.
(c) $\qquad$ anxiety has undermined his health.
(d) It is a $\qquad$ lie.

Read the paragraph and answer the question given below :
24. The global anti-ageing market is worth at least $\$ 250$ billion - an astonishing amount, and it's growing. Anti-ageing treatments are supposedly used to correct 'premature ageing'. But what does this really mean? Surely ageing is just ageing. It is a process that occurs over time- at the time that it's supposed to.
(i) The word 'premature' is used in the passage to mean:
(ii) What is meant by the 'anti-ageing market' and what is it worth?
25. We do not know how to manage our machines. Machines were made to be man's servants: yet he has grown so dependent on them that they are in a fair way to become his masters. Already most men spend most of their lives looking after and waiting upon machines. And machines are very stern masters. They must be fed with coal, and given petrol to drink, and oil to wash with, and must be kept at the right temperature, and if they do not get their meals when they expect them, they grow sulky and refuse to work, or burst with rage, and blow up and spread ruin and destruction all around them.
(i) What has gone wrong in man's handling of machines?
(ii) What does "stern masters" mean?
26. Bacon calls the riches, the baggage of virtue:

For, as the baggage is to an army, so riches are to virtue. They cannot be spread nor left behind. Yet only hinder the march. Wealth brings care in its train. Pride goes with it. And where there is pride, there can be no real virtue.

What did Christ say of a rich man? "Verily, I say unto you, it is easier for a camel to go through the eye of a needle, than for rich man to enter the Kingdom of God".
(i) Riches are called the baggage of virtue. Why?
(ii) It is difficult for a man of riches to get into the kingdom of God. Why?
( $8 \times 2$ = 16 Marks)
III. Answer any six of the following questions:
27. Fill in the blanks with the correct option
(a) He was asked to take his aged mother to see a $\qquad$ physician. (paediatric / geriatric)
(b) The server at the bank was $\qquad$ by cybercriminals. (morphed / hacked)
(c) Prof. Harvey uses a lot of scientific $\qquad$ in his speeches. (jokes / jargon)
(d) I'm just waiting for my father's nod of $\qquad$ so that I can go abroad to work.
(assent / asset)
28. Fill in the blanks with suitable phrases from those given in brackets (make up, turned up, went off, ran out, called off, look into, look up, look for)
(a) The workers $\qquad$ the strike.
(b) The boys $\qquad$ at the stroke of the ball.
(c) Surprisingly, very few guests $\qquad$ for the wedding.
(d) A bomb $\qquad$ near the park yesterday.
29. Correct the error in four of the following sentences:
(a) More than one attempt were made to rush on to the stage.
(b) The Central Government not only provided the funds but the personnel also.
(c) His wife, as well as his children are ashamed of him.
(d) John thinks he is superior than everybody else.
30. Fill in the blanks with the correct option
(a) All kinds of foreign consumer brands are now available at our store, because of the $\qquad$ policy (loacalisation / liberalisation)
(b) His decision to relocate to his native town was a $\qquad$ one.
(judicious / judicial)
(c) Why don't you $\qquad$ me instead of sending long e mails? (next / text)
(d) The story is about two families that have an ongoing $\qquad$ that goes back three generations. (food / feud).
31. Fill in the blanks with suitable phrases from those given in brackets:
(step down, held up, gave up, cut off, made up, found out)
(a) The energy company' $\qquad$ our electricity because we didn't pay.
(b) 1 $\qquad$ playing football a long time ago because of a knee injury.
(c) The Prime Minister has decided to $\qquad$ after 10 years in office.
(d) The traffic on the motorway was $\qquad$ by construction work.
32. Correct the error, if any, in the section in italics in four of the following sentences :
(a) I have spoken to him, but what he could do is another matter.
(b) Dr. Shah will be leading the surgical team, will he?
(c) I am supposed to join you at two in the afternoon, aren't I?
(d) Don't she know that she has a seminar presentation tomorrow?
(e) You don't walk on the grass, the signboard says.
33. Fill in the blanks with the suitable pronouns from those given in brackets :
(they, he, me, our, you, it, they, them, its, mine, him)
(a) You are stronger than $\qquad$
(b) I looked behind $\qquad$
(c) He said he had reported the incident to two constables but that none of
$\qquad$ was willing to intervene.
(d) Nobody but $\qquad$ was present.
(e) There were doors all around the hall, but $\qquad$ were all locked.
(f) My parents like Latin music. The CD is for $\qquad$
(g) Here is another souvenir. I don't know what to do with $\qquad$
(h) Dad is coming with $\qquad$ to buy school supplies.
34. Correct the error in the sections in italics:
(a) She must has been on holiday.
(b) Vani is as tall as all other girls in her class.
(c) Your college is good, but mine is best.
(d) It rains heavily in Assam, is'nt it?
35. Fill in the blanks with suitable words from those given in brackets :
(failure, contact, agonisingly, crash-landed, probe, journeying, successfully)

Over the weekend, India attempted to make history by becoming just the fourth nation to $\qquad$ land a $\qquad$ on the Moon. It came $\qquad$ close, but after $\qquad$ millions of kilometres, Vikram lander lost
$\qquad$ in the final few hundred metres and $\qquad$ on the lunar surface. But it would be both unfair and plain wrong to label the mission a
$\qquad$
36. Fill in the blanks with suitable words from those given in brackets: (alarmed, embodiment, ambitious, necessities, sceptical, melancholic, improved, revoked)
(a) The Manager says that the order cannot be $\qquad$
(b) We should use $\qquad$ varieties of seeds to increase production of grains.
(c) Bruto was an unselfish worker. Yet people said that he was $\qquad$
(d) His father is $\qquad$ about the son getting a top rank.
(e) The residents were $\qquad$ by the fury of the storm.
(f) The music had a $\qquad$ touch.
(g) Many of the villages in India do not even have the bare $\qquad$ of life.
(h) Mother Teresa is regarded as an $\qquad$ of kindness and love.
37. Read the passage and answer the questions given below:

Raman was a voracious reader and pored eagerly over all books in his father's collection, among which were original writings of great scientists. These books were to him like old friends, never to be forgotten. He once said, 'Out of this welter of subjects and books, can I pick anything really to mould my mental and spiritual outlook and determine my chosen path'?
(i) $\qquad$ in the passage means 'highly enthusiastic'.
(ii) 'Pored eagerly over' means $\qquad$
(a) read with great interest
(b) studied carefully
(c) both (a) and (b)
(d) skimmed trough
(iii) In the given passage, 'mould' is related to
(a) the smithy
(b) pottery
(c) baking
(d) character
(iv) 'Welter' means $\qquad$
38. Read the passage and answer the questions given below:

There has never been conceived or made by man any instrument, machine or contrivance, capable of such diversity of usefulness as the human hand. Nothing has ever existed with such infinite adaptability to various need, or capable of being trained to such degrees of dexterity and versatility. Nor is it likely that as perfect a machine, will ever be produced by human skill, for the only thing, the human hand cannot do is, to create an instrument as perfect as itself.
(i) Why is the human hand so useful?
(ii) 'Adaptability' means $\qquad$
(iii) $\qquad$ in the passage means 'an apparatus using mechanical power and having several parts, each with a definite function and together performing a particular task'.
(iv) Can as perfect an instrument as the human hand be ever created by man?
(a) Can be created.
(b) There are similar instruments as useful as the human hand.
(c) Human hand or mind is incapable of making a similar machine as human hand.
( $6 \times 4=24$ Marks)
IV. Answer any two of the following questions, choosing one from each group.
GROUP - A
39. Read the following passage and answer the questions given below:

Once the casting is done, I am ready to plunge headlong into the business of shooting. The studios of Calcutta show their hallowed past in every crevice in the wall, in every tatter on the canvas that covers the ceiling. Some of the families of rodents that inhabit the rafters have lived there ever since the foundation of the industry. The floor is pitted, the camera groans as it turns, the voltage begins to drop after sundown. The general air of shabbiness is unnerving. And yet I do not mind these at all. I do not think of these as hindrances. After all, we have the essentials to make a film, and it is within us to make it badly or well. It is the bareness of means that forces us to be economical and inventive, and prevents us from turning craftsmanship into an end in itself. And there is something about creating beauty in the circumstances of shoddiness and privation that is truly exciting...Yes, I am happy to be working where I am.

1. 'Plunge headlong into' means $\qquad$
(a) dive into water
(b) bang your head
(c) to get fully involved
(d) none of the above
2. 'Hallowed' is closest in meaning to $\qquad$
(a) holy
(b) hollow
(c) ancient
(d) unknown
3. $\qquad$ is a synonym for 'creative'.
4. Another word from the passage that is close in meaning to 'shabbiness' is $\qquad$
5. 'Privation' is a word related to $\qquad$
(a) privatisation
(b) privacy
(c) piracy
(d) deprivation
6. 'Tattered' is related $\qquad$
(a) paper
(b) cloth
(c) noise
(d) music
7. The word opposite in meaning to the word 'pitted' is
(a) smooth
(b) rough
(c) full of holes
(d) clean
8. The word that is spelt correctly is
(a) privetisation
(b) shoddiness
(c) craftmanship
(d) crivice
9. The word that is spelt wrongly is : $\qquad$
(a) ceiling
(b) voltage
(c) hinderance
(d) business

Find the synonym of the words in Italics :
10. She cried copious tears when she lost her new shoes.
(a) vast
(b) copying
(c) plentiful
(d) messy
11. They burned the effigy of the despot in the town square.
(a) dummy
(b) poster
(c) reflection
(d) statue

Find the antonyms of the words in italics :
12. February 14 was set as a tentative date for the wedding.
(a) temporary
(b) final
(c) casual
(d) convenient
13. I must say you look very urbane in this suit.
(a) elegant
(b) slow
(c) crude
(d) foolish

Choose the most suitable one-word substitute for the phrase in italics :
14. Satyajit Ray is a world famous Bengali film director who is involved in all the audio- visual elements of his films.
(a) producer
-(b) actor
(c) author
(d) auteur
15. Find the meaning of the word 'hindrance' from the passiage given above and use it in a sentence of your own.
40. Spot the error in the underlined sections in the following sentences. If there is no error, the answer is 'd'

1. You may go to your classes now, The Teacher said. No error
a
b
C
d
2. Ravi asked Megha whether she is submitted her assignment a
b
the class teacher. No error
c
d
3. 'i will not go into the hall until Resmi comes', said Jyothi. No error.
a
b
c
d
4. 'Where did you lose your purse', asked my mother. No error.
a
b
c
d
5. The group promised that they would meet again next year. No error
a
b
c
d
6. Twenty hundred weights make one ton. No Error.
a
b
c
d
7. All the three commander-in chiefs are meeting the President today. a
b
c
No error.
d
8. I who your leader will give the signal. No error.
a
b
c
d
9. Nothing is given for nothing. No error.
a
b
c
d
10. Let you and he go together. No error.
a
b
c d
11. He failed in he attempted. No error. $\begin{array}{llll}a & b & c & d\end{array}$
12. He knows better than to quarrel. No error.
$a \quad b$
b c
c .
13. Few Indian towns are so big as Madras. No error.
a
b
C
d
14. Why should I suspected by you. No error.
a b
C
d
15. Either he or I are mistaken. No error.
a
b
c
d
16. Read the passage and answer the questions given below:

Monday morning found Tom Sawyer miserable. Monday morning always found him so-because it began another week's slow suffering in school. He generally began that day with wishing he had had no intervening holiday, it made the going into captivity and fetters again so much more odious. Tom lay thinking. Presently it occurred to him that he wished he was sick; then he could stay home from school. Here was a vague possibility. He canvassed his system. No ailment was found, and he investigated again. This time he thought he could detect colicky symptoms, and he began to encourage them with considerabie hope. But hey soon grew feeble, and presently died wholly away. He reflected further. Suddenly he discovered something. One of his upper front teeth was loose. This was lucky; he was about to begin to groan as a 'starter', as he called it, when it occurred to him that if he came into court with that argument, his aunt would pull it out, and that would hurt. So he thought he would hold the tooth in reserve for the present, and seek further. Nothing offered for some little time, and then he remembered hearing the doctor tell about certain thing that laid up a patient for two or three weeks and threatened to make him lose a finger. So the boy eagerly drew his sore toe from under the sheet and held it up for inspection. But now he did not know the necessary symptoms. However, it seemed well worthwhile to chance it, so he fell to groaning with considerable spirit.

1. The word 'reflected' in the passage is closest in meaning to :
(a) consider
(b) echoed
(c) returned
(d) replicated
2. The phrase 'canvassing the system' in the passage means:
(a) appeal
(b) campaign
(c) fight
(d) check
3. The word in the passage which is the opposite of 'pleasing' is :
(a) suffering
(b) intervening
(c) colicky
(d) odious
4. Identify the statement which is true :
(a) Tom thought it was bad luck to have a shaky front tooth
(b) Tom hated being sick
(c) Tom began to encourage the colicky pain with hope
(d) None of the above
5. Monday morning found Tom Sawyer miserable. Why?
(a) Tom was feeling colicky
(b) Tom had a tooth ache
(c) Tom was scared of going to the doctor
(d) Tom did not like going to school
6. Why did Tom wish he had had no intervening holiday?
(a) It made going back to school so much more hateful
(b) Tom did not want to stay at home
(c) School was always great fun for Tom
(d) All of the above
7. "Ailment" means $\qquad$
8. The synonym for "fetters" is
(a) fritters
(b) chains
(c) fight
(d) check
9. By which phrase does Tom describe his experience in school?
10. The word "sore" in the phrase "sore toe" means
(a) big
(b) broken
(c) letters
(d) none of the above
11. Why did Tom canvass his system?
12. Why did Tom hold up the sore toe for inspection?
13. What was the 'starter' for Tom Sawyer?
14. Based on the incident mentioned here, comment briefly on the character of Tom Sawyer?
1.5. Suggest a suitable title for the passage.
GROUP - B
15. Answer all the following questions:

Fill in the blanks with suitable tense forms of the verbs given in brackets :

1. Nadella $\qquad$ (choose) to join Microsoft because he $\qquad$ (want) to make a difference.
2. It $\qquad$ (be) an honour for him to lead and serve the company.
3. We $\qquad$ (go) for a movie yesterday. $\qquad$ (Do) you
____ (know) that my friend's daughter ______ (act) in that movie? She -_ (play) the role of the heroine's younger sister, but it $\qquad$ (be) an important role. None of us (expect) her to do so well, but she __ (do) a great job. I ___ (hear) that she even ____ an award for her role. Our club $\qquad$ (host) a reception for her when she $\qquad$ (come) to our town next month.

Fill in the blanks with suitable prepositions:
4. He warned you _ _ . . . the danger; but you did not listen -_ him.
5. France is famous - _- its perfumes. You are looking some —__ _ the most expensive brands available this country.
6. This company deals ___ electronic goods. Ajay's been working here as Manager ___ two years now.
7. Rewrite the following sentence into active voice :
(a) Cricket is played in most countries today.
(b) Will you be supported by your friends in this venture?
43. Read the passage and answer the questions given below:

Muhammad Yunus, the founder of Grameen Bank, is a Bangladeshi banker, author and economist whose focus on microcredit and microfinance concepts led to him being awarded the Nobel Price in 2006 for efforts to create economic and social development from below'. Yunus was born in 28 June 1940 in Chittagong. His father was jeweler and his mother was his role model; a women who helped anyone that knocked on their door. After high school and college, Yunus completed his PhD in Economics in the US and worked as an assistant professor of Economics till 1972, when he returned to Bangladesh. It was during this time that Yunus would stumble across an idea that lead to him helping millions of poverty people and would lead to him being awarded the Nobel Prize.

In 1974, Bangladesh suffered from a famine, resulting from rain and massive flooding that devastated crops. And the people of Bangladesh received no relief or aid from other countries. Yunus began to be actively involved in poverty reduction. He established a rural economic program as a research project and visited the poorest households in a village near Chittagong. He interviewed a woman who was making bamboo stools and learnt that she was being charged
exorbitant rates for her loans, and thus was barely making a profit. He realized the potential for recovery then and there and in an exhibition of practical economics, loaned the equivalent of twenty-seven US dollars to forty-two women in the village. It was his first loan. With more advantageous rates, these women were able to raise their profits and manage better than before. Without these new rates, the women would likely have been stuck in a rut for the rest of their lives. Yunus realized that on a smaller scale, microfinance and microcredit could really help Bangladesh's struggle with poverty.

1. The prefix $\qquad$ is used in the passage for 'small scale'
2. The word 'devasted' means $\qquad$
(A) Devoid
(B) Desperate
(C) Destroyed
(D) Deserted
3. The phrase that means 'without any change or improvement' is
$\qquad$
4. The phrase 'from below' in the first sentence is used in the sense of
(A) Below sea level
(B) From a disadvantaged country
(C) Below poverty line
(D) None of the above
5. The word closest in meaning to "exorbitant" is $\qquad$
(A) Ineffective
(B) Expected
(C) Easily available
(D) Highly priced
6. The word 'rates' is related to $\qquad$
(A) Cost
(B) Interest
(C) Profit
(D) Loss
7. The word that is the antonym of 'urban' is $\qquad$
8. 'Exhibition of ' means $\qquad$
(A) Display
(B) Open Mindedness
(C) Expression
(D) None of the above
9. The wrongly spelt word is :
(A) Exorbitant
(B) Advantageus
(C) Microcredit
(D) Potential
10. The correctly spelt word is :
(A) Povertystruck
(B) Exhibition
(C) Famin
(D) Poverty Stricken
11. I suppose the headmaster himself will $\qquad$ the matter now.
(A) Look into
(B) Look at
(C) Look out for
(D) Look up
12. In spite of our best efforts at secrecy, my mother $\qquad$ our plans for a surprise party.
(A) Turn up
(B) Got wind of
(C) Caught up with
(D) Wound up
13. A person who studies human cultures and societies is $\qquad$
(A) A philologist
(B) An archaeologist
(C) An anthropologist
(D) A linguist
14. Correct the spelling of the following word and make a sentence of your own 'necessity'.

Find the antonyms of the words in italics :
15. Escalating prices cause hardship to the poor
(A) Fixed
(B) Falling
(C) Reasonable
(D) Fluctuating
44. Answer all the following questions :

Fill in the blanks with suitable modal auxiliaries from the list given below :
(will, would, should, can, must, might, need, dare, used to)

1. Sara $\qquad$ to do some exercises for her shoulder, otherwise she
$\qquad$ need a surgery.
2. You $\qquad$ have spoken rudely to her, otherwise she $\qquad$ not have left soon.
3. $\qquad$ you sing a song for Tara's birthday? You $\qquad$ sing so well when we were in school.
4. I $\qquad$ not climb up the hill, it $\qquad$ be slippery after such heavy rain.
5. $\qquad$ you be coming tomorrow? We really $\qquad$ complete that file.

Complete the following sentences with suitable verbs and corresponding question tags :
6. You aren't coming to college tomorrow, $\qquad$ ?
7. Rahman $\qquad$ the boy who stood first in class, isn't he?
8. Jaya goes to the library every Saturday, $\qquad$ ?
9. Let us all go for a movie next Sunday, $\qquad$ ?
10. $\qquad$ as tall as Rosy, aren't I?

Insert the adverb given in brackets in the correct position in the sentence :
11. She impressed him by her singing. (greatly)
12. There was nothing to do but wait for the next bus to arrive. (else)
13. He admires my clothes (always)
14. This room is big enough for all of us to sleep in. (enough)
15. The new tax structure is tough on the middle classes. (rather)

Reg. No. : $\qquad$
Name : $\qquad$
Third Semester B.Sc. Degree Examination, March 2021 First Degree Programme Under CBCSS

Mathematics

## Core Course

## MM 1341 - ELEMENTARY NUMBER THEORY AND CALCULUS - I

(2019 Admission Regular)
Time: 3 Hours
PART - A

Answer all questions from $\mathbf{1}$ to $\mathbf{1 0}$. Each question carries 1 mark.

1. State the division algorithm.
2. State the pigeonhole principle.
3. If $r(t)=t^{2} i+e^{t} j-(2 \cos \pi t k)$, find $r^{\prime}(t)$.
4. Evaluate the definite integral $\int_{0}^{2}\left(2 t i+3 t^{2} j\right) d t$.
5. Write the formula for finding the arc length of a parametric curve $x=x(t)$, $y=y(t), a \leq t \leq b$.
6. Find a parametrization of the cone $z=\sqrt{x^{2}+y^{2}}, 0 \leq z \leq 1$.
7. Let $f(x, y)=\sqrt{y+1}+\ln \left(x^{2}-y\right)$. Find $f(e, 0)$.
8. Evaluate $\lim _{(x, y) \rightarrow(-1,2)} \frac{x y}{x^{2}+y^{2}}$.
9. Find $\frac{\partial w}{\partial x}$ if $w=2 y e^{z} \sin x z$.
10. Define the gradient of the function $f(x, y, z)$.
PART - B

Answer any eight questions from 11 to 26 . Each question carries 2 marks.
11. Let $b$ be an integer $\geq 2$. Suppose $b+1$ integers are randomly selected. Prove that the difference of two of them is divisible by $b$.
12. State the Inclusion Exclusion principle.
13. If $a \mid c$ and $b \mid c$, and $(a, b)=1$, show that $a b \mid c$.
14. If $p$ is a prime and $p \mid a b$, show that $p \mid a$ or $p \mid b$.
15. Sketch the graph and a radius vector of $r(t)=\cos t i+\sin t j, 0 \leq t \leq 2 \pi$.
16. Find the arc length of that portion of the circular helix $x=\cos t, y=\sin t, z=t$ from $t=0$ to $t=\pi$.
17. Determine whether $r(t)=t^{3} i+\left(3 t^{2}-2 t\right) j+5 t^{2} k$ is smooth or not.
18. Find the unit tangent vector to the graph of $r(t)=t^{2} i+t^{3} j$ at the point $t=2$.
19. Find the instantaneous velocity and speed of a particle that moves in a circular path such that its $x$ and $y$ coordinates at time $t$ are $x=2 \cos t$, and $y=2 \sin t$.
20. Find the curvature of a circle of radius $a$.
21. Evaluate $\lim _{(x, y) \rightarrow(0,0)} \frac{-x y}{x^{2}+y^{2}}$ along the parabola $y=x^{2}$.
22. Find $f_{x}$ and $f_{y}$ for $y(x, y)=2 x^{3} y^{2}+2 y+4 x$.
23. Show that $f(x, y)=x^{2}+y^{2}$ is differentiable at $(0,0)$.
24. Using the chain rule find $d z / d t$ if $z=x^{2} y, x=t^{2}, y=t^{3}$.
25. Let $f(x, y)=x^{2} e^{y}$. Find the maximum value of a directional derivative at $(-2,0)$ and find the unit vector in the direction in which the maximum value occurs.
26. Find the equation of the tangent plane to the ellipsoid $x^{2}+4 y^{2}+z^{2}=18$ at the point (1, 2, 1).
PART-C

Answer any six questions from 27 to 38 . Each question carries 4 marks.
27. Let $a$ and $b$ be any positive integers. Show that the number of positive integers $\leq a$ and divisible by $b$ is $[a / b]$.
28. Find the primes such that the digits in their decimal values alternate between 0 's and 1 's, beginning with 1 and ending in 1.
29. Let $f_{i}$ denote the $i$-th Fermat number. Show that $f_{0} f_{1} \ldots f_{n-1}=f_{n}-2$, where $n \geq 1$.
30. Show that there are infinitely many primes of the form $4 n+3$.
31. The graphs of $r_{1}(t)=\left(\tan ^{-1} t\right) i+(\sin t) j+t^{2} k$ and $r_{2}(t)=\left(t^{2}-t\right) i+(2 t-2) j+\ln t k$ intersect at the origin. Find the degree measure of the acute angle between the tangent lines to the graphs of $r_{1}(t)$ and $r_{2}(t)$ at the origin.
32. Find $T(t)$ and $N(t)$ for the circular helix $x=a \cos t, y=a \sin t, z=c t$, where $a>0$.
33. Find the curvature and radius of curvature of $r(t)=5 \cos t i+12 \sin t j+t k$ at $t=\pi / 2$.
34. Find the arc length parametrization of the circular helix $r=\cos t i+\sin t j+t k$ that has reference point $r(0)=(1,0,0)$ and the same orientation as the given helix.
35. Confirm that the mixed partial derivatives of $f(x, y)=4 x^{2}-8 x y^{4}+7 y^{4}-3$ are equal.
36. Suppose that $w=\sqrt{x^{2}+y^{2}+z^{2}}, x=\cos \theta, y=\sin \theta, z=\tan \theta$. Use the chain rule to find $d w / d \theta$ when $\theta=\pi / 4$.
37. Find the directional derivative of $f(x, y)=e^{x y}$ at $(-2,0)$ in the direction of the unit vector that makes an angle $\pi / 3$ with the positive axis.
38. Find the parametric equations of the tangent line to the curve of intersection of the paraboloid $z=x^{2}+y^{2}$ and the ellipsoid $3 x^{2}+2 y^{2}+z^{2}=9$ at the point (1, 1, 2).

## PART - D

Answer any two question from 39 to 44 . Each question carries 15 marks.
39. (a) State and prove the fundamental theorem of arithmetic.
(b) Show that the linear Diophantine equation (LDE) $a x+b y=c$ is solvable if and only if $d / c$, where $d=(a, b)$. Also show that If $x_{0}, y_{0}$ is a particular solution of the LDE, then all its solutions are given by $x=x_{0}+\left(\frac{b}{d}\right) t$, $y=y_{0}-\left(\frac{a}{d}\right) t$ where $t$ is an arbitrary integer.
40. (a) Let $\alpha=\frac{1+\sqrt{5}}{2}$. Show that $\alpha^{n-2}<F_{n}<\alpha^{n-1}$, where $n \geq 3$ and $F_{n}$ denotes the $n$-th Fibonacci number.
(b) Show that the number of divisions needed to compute ( $a, b$ ) by the eu-clidean algorithm is at most five times the number of decimal digits in $b$, where $a \geq b \geq 2$.
41. (a) The length, width and height of a rectangular box are measured with an error of at most $5 \%$ Use a total differential to estimate the maximum percentage error that results if these quantities are used to calculate the diagonal of the box.
(b) Let $L(x, y)$ denote the local linear approximation to $f(x, y)=\sqrt{x^{2}+y^{2}}$ at the point $(3,4)$. Compare the error in approximating $f(3.04,3.98)$ by $L(3.04,3.98)$ with the distance between the points $(3,4)$ and $(3.04,3.98)$.
42. Suppose that a particle moves through 3-space so that its position vector at time $t$ is $r(t)=t i+t^{2} j+t^{3} k$.
(a) Find the scalar tangential and normal components of acceleration at time $t$.
(b) Find the scalar tangential and normal components of acceleration at time $t=1$.
(c) Find the vector tangential and normal components of acceleration at time $t=1$.
(d) Find the curvature at the point where the particle is located at time $t=1$.
43. (a) Find the absolute maximum and minimum values of $f(x, y)=3 x y-6 x-3 y+7$ on the closed triangular region $R$ with vertices $(0,0),(3,0)$ and $(0,5)$.
(b) Consider the ellipsoid $x^{2}+4 y^{2}+z^{2}=18$.
(i) Find an equation of the tangent plane to the ellipsoid at the point (1, 2, 1).
(ii) Find parametric equations of the line that is normal to the ellipsoid at the point $(1,2,1)$.
(iii) Find the acute angle that the tangent plane at the point (1, 2,1 ) makes with the $x y$-plane.
44. (a) Locate all relative extrema and saddle points of $f(x, y)=4 x y-x^{4}-y^{4}$.
(b) Find the points on the sphere $x^{2}+y^{2}+z^{2}=36$ that are closest to and farthest from the point $(1,2,2)$.

Reg. No.: $\qquad$
$\qquad$

# Third Semester B.Sc. Degree Examination, March 2021 

First Degree Programme under CBCSS
Statistics
Complementary Course For Mathematics
ST 1331.1 - STATISTICAL DISTRIBUTIONS
(2018 Admission)
Time: 3 Hours
Max. Marks : 80
Use of statistical table and scientific calculator are permitted.
SECTION - A

Answer all questions. Each question carries 1 mark.

1. What are the parameters of a binomial random variable with mean 4 and variance 3 ?
2. Find the coefficient of variation of Poisson distribution with mean 9 .
3. If $X$ is a Poisson variable such that $P(X=1)=P(X=2)$, obtain $P(X=0)$.
4. If $X$ and $Y$ are independent uniform random variables over $[0,2]$, determine $P(X<Y)$.
5. State the distribution of $Z=X+Y$, where $X$ and $Y$ are independent standard normal variables.
6. Define exponential distribution.
7. Define type II beta distribution.
8. What do you mean by sampling distribution?
9. State the distribution of the ratio of two independent standard normal variables.
10. Define statistic.

$$
\text { ( } 10 \times 1=10 \text { Marks) }
$$

## SECTION-B

Answer any eight questions. Each question carries 2 marks.
11. Define Bernouili random variable.
12. Define hypergeometric distribution.
13. The ratio to 3 successes and 4 successes among seven independent Bernoullian trials is $\frac{1}{4}$. Find the probability of success.
14. If $X$ follow uniform distribution with mean 1 and variance $\frac{4}{3}$, find $P(X<0)$.
15. If $X \sim N(6,2)$, find $P(1<X<3)$
16. A horizontal line of length 5 units is divided by a point chosen at random into two parts. If the length of the first part is $X$, find $E[X(5-X)]$.
17. What are the advantages of Chebychev's inequality?
18. What are the conditions for Lindberg-Levy form of central limit theorem?
19. Find the mean of a random variable following chi-square distribution with $n$ degrees of freedom.
20. A• random sample of size 25 is taken from $N(1,9)$. What is the probability that the sample mean is negative?
21. State Bernoulli's weak law of large numbers.
22. Let $X_{1}, X_{2}, \ldots, X_{n}$ are independent exponential random variables with parameter $\lambda$. Show that $X=X_{1}+X_{2}+\ldots+X_{n}$ follows gamma distribution.

$$
(8 \times 2=16 \text { Marks })
$$

## SECTION - C

Answer any six questions. Each question carries 4 marks.
23. If $X \sim B(n, p)$, show that $\operatorname{Cov}\left(\frac{X}{n}, \frac{n-X}{n}\right)=\frac{-p q}{n}$.
24. If $X$ follows Poisson distribution with parameter unity, show that mean deviation about mean is $\frac{2}{e}$ times the standard deviation.
25. If $X$ and $Y$ are independent geometric variables with same parameter, find the conditional distribution of $X \mid X+Y$.
26. In a normal distribution $30 \%$ of the items are above 42 and $30 \%$ of the items are below 28. What are the mean and standard deviation of the distribution?
27. Derive the moment generating function of normal distribution.
28. If $X$ follows beta distribution of the first kind with parameters. $p$ and $q$, show that $Y=\frac{X}{1-X}$ follow beta distribution of the second kind.
29. In a die throwing experiment using an unbiased die, $\ddot{x}$ denotes the number shown by the die. Using Chebychev's inequality, prove that $P(|X-\mu|>2.5)<0.47$.
30. For a random sample of size 16 from $N\left(\mu, \sigma^{2}\right)$ population the sample variance is 16. Find $a$ and $b$ such that $P\left(a<\sigma^{2}<b\right)=0.6$.
31. If $X \sim N(0,1)$, prove that $Y=X^{2}$ follow chi-square distribution with one degree of freedom.
( $6 \times 4=24$ Marks)

## SECTION - D

Answer any two questions. Each question carries 15 marks.
32. The numbers of printing errors per page reported in a book with 1000 pages published by a good published were noted.

| No. of mistakes | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of pages | 626 | 285 | 65 | 15 | 6 | 2 | 1 | 0 | 0 |

Fit a Poisson distribution and calculate the theoretical frequencies.
33. State and prove the recurrence relation for central moments of a binomial distribution.
34. Derive the expression for central moments of a normal distribution.
35. If $X$ is a random variable following F-distribution with $\left(n_{1}, n_{2}\right)$ degrees of freedom. Show that $Y=\frac{1}{X}$ follows $F$-distribution with $\left(n_{2}, n_{1}\right)$ degrees of freedom.

Reg. No. : $\qquad$
Name : $\qquad$

# Third Semester B.A./B.Sc. Degree Examination, March 2021 First Degree Programme Under CBCSS 

Hindi
Language Course - (Additional Language - III)
HN 1311.1 - POETRY AND GRAMMAR
(2019 Admission Regular)

## Time : 3 Hours

।. एक या दो वाक्यों में उत्तर लिखिए।

1. सूरदास के गुु कौन है ?
2. हिन्दी किस लिपि में लिखी जाती है ?
3. अष्टछाप की स्थापना किमने की ?
4. तुलसीदास के बचपन का नाम क्या है?
5. ताग्सप्तक के सम्पादक कौन थे ?
6. राष्ट्रकवि की उपाधि से सम्मानित कवि कौन है?
7. उजाला किसकी ग्नना है ?
8. 'लड़का' शब्द का भाववाचक संज्ञा लिखिए।
9. नागार्जुन ने मैथिली में किस नाम से लेख़्बनी चलाई?
10. छायावाद के चार स्तभं कौन-कौन है ?
(10×1 = 10 Marks)
II. किन्हीं आठ प्रश्नों का उत्तर दो या तीन वाक्यों में लिखिए।
11. कबीरदास ईश्वर मे भी अधिक महत्व किस को देते है? क्यों?
12. दूध पिलाने के लिए ग्रशोदा कृष्ण को क्या प्रलोभन देती है ?
13. तुलसीदास क्यों कहते हैं कि सन्त आम के पेड के समान है ?
14. "जाति न पूछो साधु की, पूछि लीजिये ज्ञान। मोल करो तलवार का, पड़ा रहन दो म्यान।" - भाव समाझाइए।
15. "आवत ही हरसे नहीं नैनन नह्दी स्नेह। तुलसी तहाँ न जाइये कंचन बरसे मेघ!" - भाव समाझाइए।
16. संज्ञा किसे कहते है ? उसंके भेद क्या-क्या है?
17. 'को' विभक्ति के विविध कारक रूपों का परिचय दीजिए।
18. भाववाचक संज्ञायें किस प्रका के शब्दों से बनती है? उदाहरण सहित लिखिए।
19. विभक्ति और कारक में क्या भेद है ?
20. आदिवासी नौजवान नदी को कैसे मलिन करता है?
21. उदयप्रकाश का लघु परिचय दीजिए।
22. यश़ोधरा क्यों दुखा है ? स्पष्ट कीजिए।
23. सुमित्रानंदन पंत क्यों कहते है कि वे चिर सुख और दुख नरीं चाहते?
24. मुरझाया फूल किसका प्रतीक है? स्पष्ट कीजिए।
25. 'सुनो हमें अऩहद की तरह

और समझो जैसे समझी जाती है
नयी-नयी सीखी हुई भाषा।"

- भाव समझाइए।

26. "शक्ति रहे तेरे हाथों में -

छूट न जाये यह चाह सृजन की
शाक्ति रहे तेरे हाथों में
रुक न जाए यह गति जीवन की।"

- भाव समझाइए।

1il. किन्हीं छः प्रश्नों का उत्तर लिखिए।
27. बाल कृष्ण अपनी माता से किस बात की शिकायत करता है ?
28. 'सुख और दुख' कविता में कवि के दार्शनिक विचाए क्या है ?
29. नैरागी के अनुसार वर्तमान मथुरा की स्थिति कैसी है ?
30. 'उड़ चल हारिल' कविता में चित्रित कर्मग्त जीवन पर प्रकाश डालिए।
31. "गोधन, गज धन, बाजि धन और रतन धन खान।

जन आवत संतोष-धन सन धन धूरि समान।"

- सप्रसंग व्याख्या कीजिए।

32. 'बुरा जो देखन में चला, बुरा न मिल्या कोय।

जो दिल खोजा आपना, मुझ से बुरा न कोय।"

- मप्रसंग व्याख्या कीजिए।

33. आदससूचक 'आप' और निज्जवाचक 'आप' में क्या अन्तर है? उदाहरण सहित लिखिए।
34. संख्यावाचक विशेषण और परिमाण वाचक विशेषण में क्या अन्तर है ?
35. स्नीलिंग संज्ञाओं के पहचान के किन्हीं पाँच नियम लिखिए।
36. 'विश्व में है फूल, तू सबके हदद्य भाता रहा, दान कर सर्वस्व भी तू हाय हर्षाता रहा।

जन न तेरी दशा पर दुखा हुआ संसार को ?
कौन रोएगग सुमन, हम से मनुज निस्सार को।"

> — सप्रसंग व्याख्या कीजिए।
37. स्वयं सुसजित करके क्षण में

प्रियतम को प्राणों के पण में,
हमें भेज देती है रण में -
क्षात्र धर्म के नाते।
— सप्रसंग व्याख्या कीजिए।
38. 'उजाला' कविता में कवि ने क्या व्यक्त किया है ?

$$
(6 \times 4=24 \text { Marks })
$$

IV. किन्हीं दो प्रश्नों के उत्तर लिखिए।
39. पठित पाठ के आधार पर कबीरदास के काव्य की विशेषताओं पर प्रकाश डालिए।
40. 'स्रियां' कविता का भाव समझाइए।
41. भिक्षुक कविता की समीक्षा कीजिए।
42. 'वह फिर जी उठी' कविता हमारे वर्तमान परिस्थिति से जुडी है। स्पष्ट कीजिए।
43. कारक की परिभाषा देकर उसके भेदों को उदाहरण सहित समझाइए।
44. सर्वनाम किसे कहते है उसके भेदों को सोदाहरण समझाइए।

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Third Semester B.Sc. Degree Examination, March 2021 First Degree Programme under CBCSS

## Physics

## Complementary Course for Mathematics

## PY 1331.1 : OPTICS, MAGNETISM AND ELECTRICITY

(2018 Admission)
Time : 3 Hours

PART - A

Answer all the questions. Answer should not exceed 2 sentences.
Each question carries 1 mark.

1. What is Fraunhoffer diffraction?
2. What is meant by grating element?
3. What are coherent sources?
4. Why Newton's rings are circular?
5. Name the active medium in a ruby laser.
6. Name four elements which exhibit ferromagnetism?
7. Define the term magnetic susceptibility.
8. What do you mean by numerical aperture?
9. What is a transformer?
10. What do you mean by wattless current?

$$
\text { (10 } \times 1=10 \text { Marks) }
$$

PART - B.

Answer any eight questions. Answer should not exceed one small paragraph.
Each question carries 2 marks.
11. Distinguish between interference and diffraction.
12. Distinguish between dispersive power and resolving power of a grating.
13. Explain constructive interference with equations.
14. What are the applications of optical fibre?
15. What is an optical pumping? Give example.
16. Explain the magnetic properties of paramagnetic materials.
17. Write note on graded index fiber.
18. Write note on ferromagnetism.
19. Comment on the magnetic susceptibility and permeability of diamagnetic materials and give examples.
20. Briefly explain about principle of light propagation in an optical fiber.
21. Write note on the Propagation Modes of optical fiber.
22. Explain the terms angle of refraction and angle of incidence.

## PART - C

Answer any six questions. Each question carries 4 marks.
23. A step index fibre has a numerical aperture of 0.20 and a cladding refractive index of 1.59 . Find the acceptance angle for the fibre in water which has a refractive index of 1.33.
24. An optical fibre has an acceptance angle $34.72^{\circ}$. Calculate its numerical aperture. If the refractive indices of core and cladding are 1.53 and 1.42. Calculate its critical angle.
25. In Fraunhoffer diffraction pattern due to a narrow slit a screen is placed 2 m away from the lens to obtain the pattern. If the slit width is 0.5 mm and the first minima lie 2 mm on either sides of the central maximum, find the wavelength of light.
26. A parallel beam of light of wavelength $6000 \AA$ is incident at an angle of $30^{\circ}$ on a plane transmission grating which has 5460 lines / cm. find the highest order spectrum that can be observed.
27. A specimen of radius 0.25 cm is kept parallel to magnetising field $4000 \mathrm{Am}^{-1}$. It acquires a pole strength of 8 Am . Calculate the magnetic susceptibility and permeability of the material.
28. A resistor of 3 ohms and a capacitor of capacity $800 \mu \mathrm{~F}$ are connected in series across 220 volts 50 cycles AC. Calculate
(a) capacitative reactance
(b) impedance
(c) current
(d) pd across the resistance
(e) pd across the capacitor
(f) the phase lag.
29. Find the value of the current through a inductance of 0.5 H when connected to an AC source of 220 V and 50 cps is applied to it.
30. Diameter of a particular dark ring in Newton Rings experiment in reflected system is 0.8 mm . When a transparent liquid of refractive index 1.6 is placed between lens and the plate, calculate the diameter of ring.
31. A series RLC circuit consists of a $12 \Omega$ resistor, a $100 \mu \mathrm{~F}$ capacitor, and a 150 mH inductor. If the source frequency is 50 Hz , calculate the total impedance.
( $6 \times 4=24$ Marks)
PART - D

Answer any two questions. Each question carries 15 marks.
32. Describe briefly about the light propagation in optical fibre and mention its applications.
33. With neat diagram explain about transformers, its different types and applications.
34. Give the theory of a plane transmission grating and describe how it is used to determine the wavelength of light, using grating at normal incidence with a neat diagram.
35. Discuss the interference in thin films-(reflected systems) and the effect of thickness of film.

$$
(2 \times 15=30 \text { Marks })
$$

Reg. No. :
Name: $\qquad$

Third Semester B.A./B.Sc. Degree Examination, March 2021 First Degree Programme under CBCSS Malayalam

Language Course - Additional Language III

(2019 Admission - Regular)
Time : 3 Hours
Max. Marks : 80



3. 'คณゅயை




 ธேோm"?


(10 $\times 1=10$ Marks)















































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Reg. No. : $\qquad$
Name: $\qquad$

# Third Semester B.Sc. Degree Examination, March 2021. 

First Degree Programme under CBCSS
Statistics Complementary Course for Mathematics

## ST 1331.1 - STATISTICAL DISTRIBUTIONS <br> (2019 Admission Regular)

Time : 3 Hours
Max. Marks : 80
SECTION - A

Answer all questions. Each question carries 1 mark :

1. What is the mean and variance of a Binomial random variable with $n=10$ and $p=0.2$.
2. What is characteristic function. Write down the characteristic function of a Poisson distribution.
3. Write down the pmf of Geometric distribution.
4. Which continuous distribution has lack of memory property?
5. What is the use of MGF?
6. Give the mean and variance of Gamma distribution.
7. State WLLN.
8. What is the limiting distribution in Central limit theorem?
9. Define raw moment.
10. Characteristic function always exist. True or False?
(10 $\times 1=10$ Marks)

## SECTION - B

Answer any eight questions. Each question carries 2 marks.
11. Define Hypergeometric distribution.
12. Obtain the mean and variance of Exponential distribution?
13. If $X \sim N(0,1)$, what is $\mathrm{P}(\mathrm{X}<1.96)$ ?
14. What is the cdf of a Exponential distributions?
15. Prove the additive property of Binomial distributions.
16. Obtain the expression for central moment in terms of raw moments.
17. State and prove Bernoulli Law of Large numbers.
18. Show that for iid random variables, sample mean converges in probability to population mean.
19. What is Chebyshev's inequality?
20. If $X$ is a Normal random variable with mean 2 and variance 2. Find $P\left(\left|X_{n}-2\right|>\sqrt{21.96}\right)$.
21. What is the pdf of Standard Normal distribution. Give mean and variance.
22. If $X$ is a random variable with distribution function $F(x)$, what are the properties of $F(x)$.
23. Obtain the moment generating function of Exponential distribution.
24. What are the first and second raw moment of Hyper-geometric distribution?
25. Show that sum of Exponential distribution follows Gamma distribution.
26. $X$ follows $N(0, I)$, Find the distribution of $Y=\frac{x-5}{2}$.

$$
(8 \times 2=16 \text { Marks })
$$

SECTION - C
Answer any six questions. Each question carries 4 marks.
27. Derive variance of Normal distribution.
28. Find mean and variance of Poisson distribution using MGF
29. Derive the distribution of sum of two Normal distribution.
30. Find the mode of the Normal distribution.
31. Explain the fitting of Binomial distributions.
32. Find the coefficient of variation of a Exponential distribution.
33. If $X$ is a continuous random variable with pdf $f(x)=\left\{\begin{array}{ll}3 e^{-3 x}, x>0 \\ 0, & \text { e/sewhere }\end{array}\right.$, then $P(X<3)=$ $\qquad$
34. If $X \sim$ Poisson(6), then find the distribution of $X+a$
35. State and prove memory less property of Exponential distribution.
36. Obtain the Poisson distribution as a limiting form of Binomial distribution.
37. Find the mean and variance of Beta distribution of first kind.
38. If $\left\{X_{i}\right\}$ is a sequence of i.i.d random variables with mean 0 and variance 1 . Show that sample mean converges in probability to 0.
( $6 \times 4=24$ Marks)

## SECTION - D

Answer any two questions. Each question carries 15 marks
39. Fit the Poisson distribution for the following data.

| $X$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 7 | 6 | 19 | 35 | 30 | 23 | 7 | 1 |

40. Show that Binomial distribution converges to Normal distribution.
41. (a) Prove the additive property of Gamma distribution.
(b) Derive the first two central moments of Normal distribution using MGF.
42. (a) What is the probability of obtaining more than 1499 heads in 1500 tosses of a fair coin.
(b) Derive the mgf of Binomial distribution and hence obtain the first three central moments.
43. (a) Show that sum and difference of two Normal random variables are Normal.
(b) Obtain the mean and variance of Geometric distribution.
44. (a) Define Uniform distribution. Derive the mean and variance.
(b) Derive the recurrence relation for probabilities of Binomial distribution.

$$
\text { ( } 2 \times 15=30 \text { Marks })
$$

